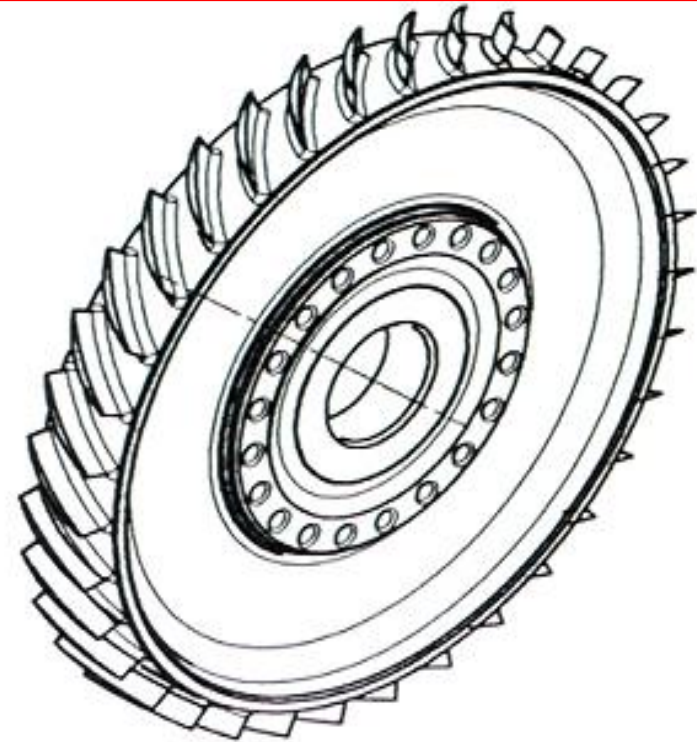
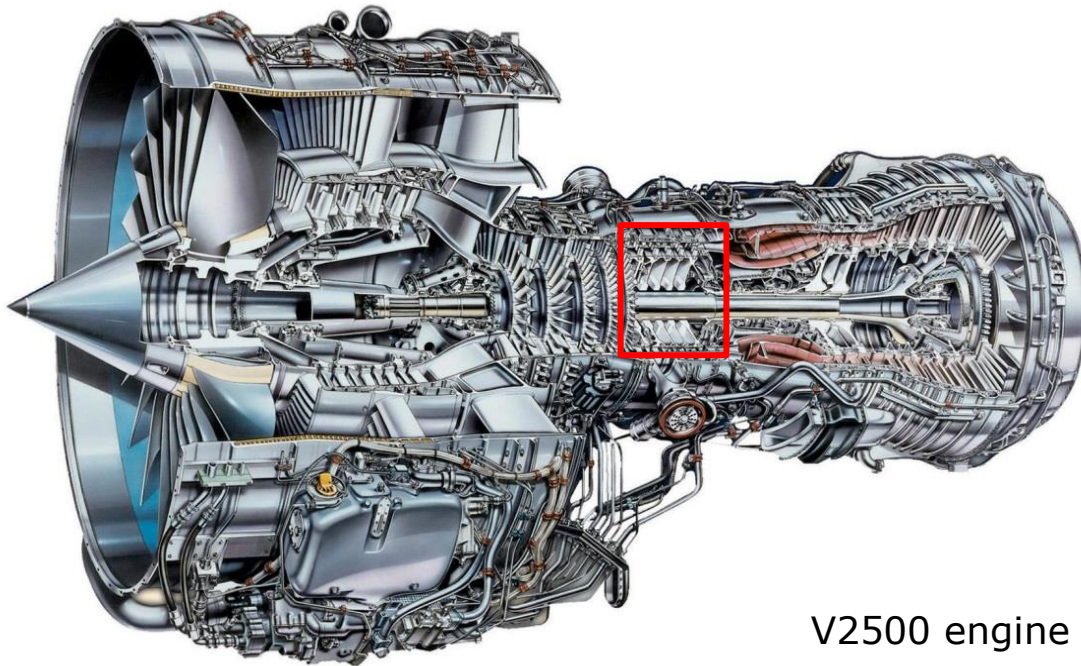
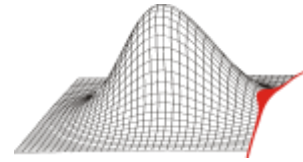
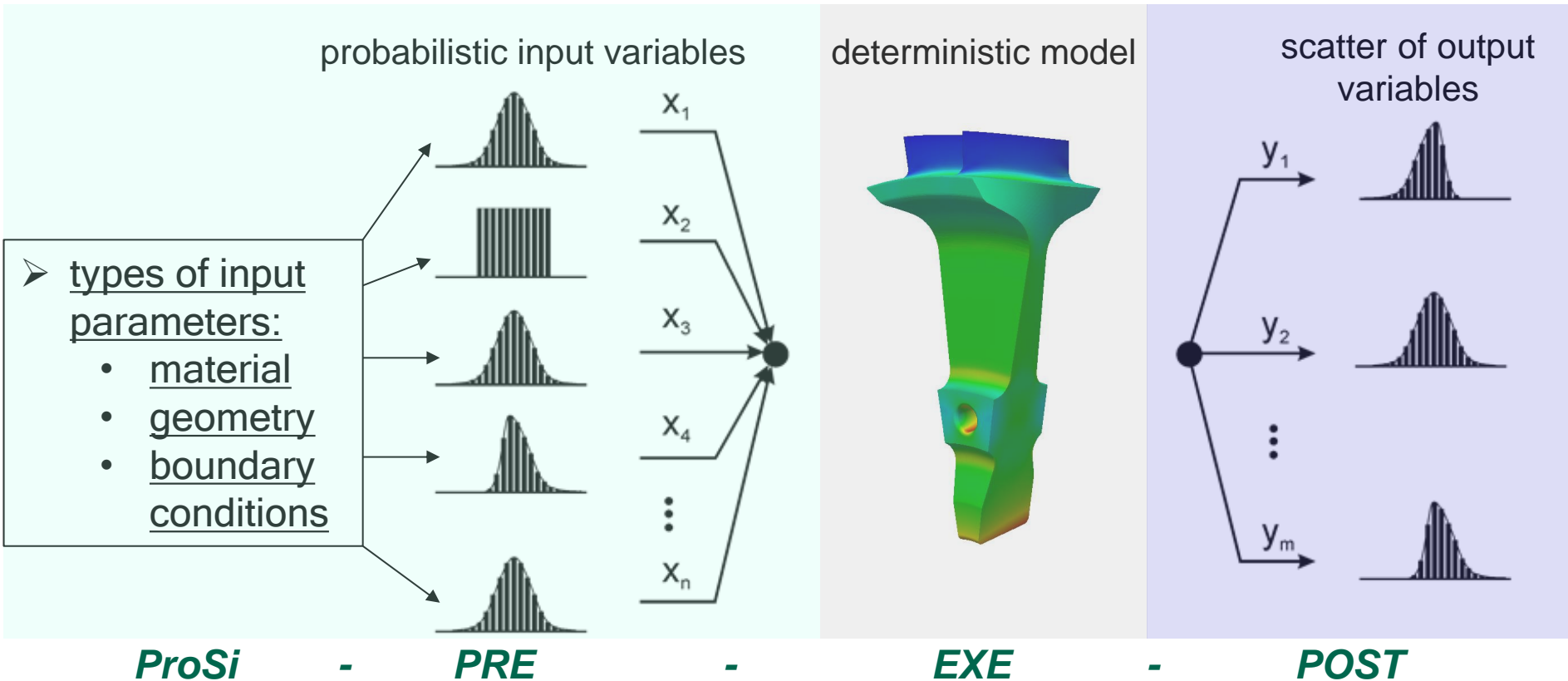
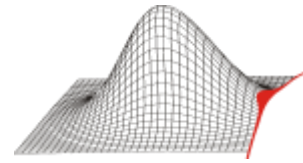


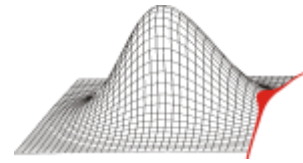
# Probabilistic Structure-Mechanical Robustness Estimation of Rotor Discs Considering Geometry Variations

I. Reuter, M. Voigt, K. Vogeler - Technische Universität Dresden

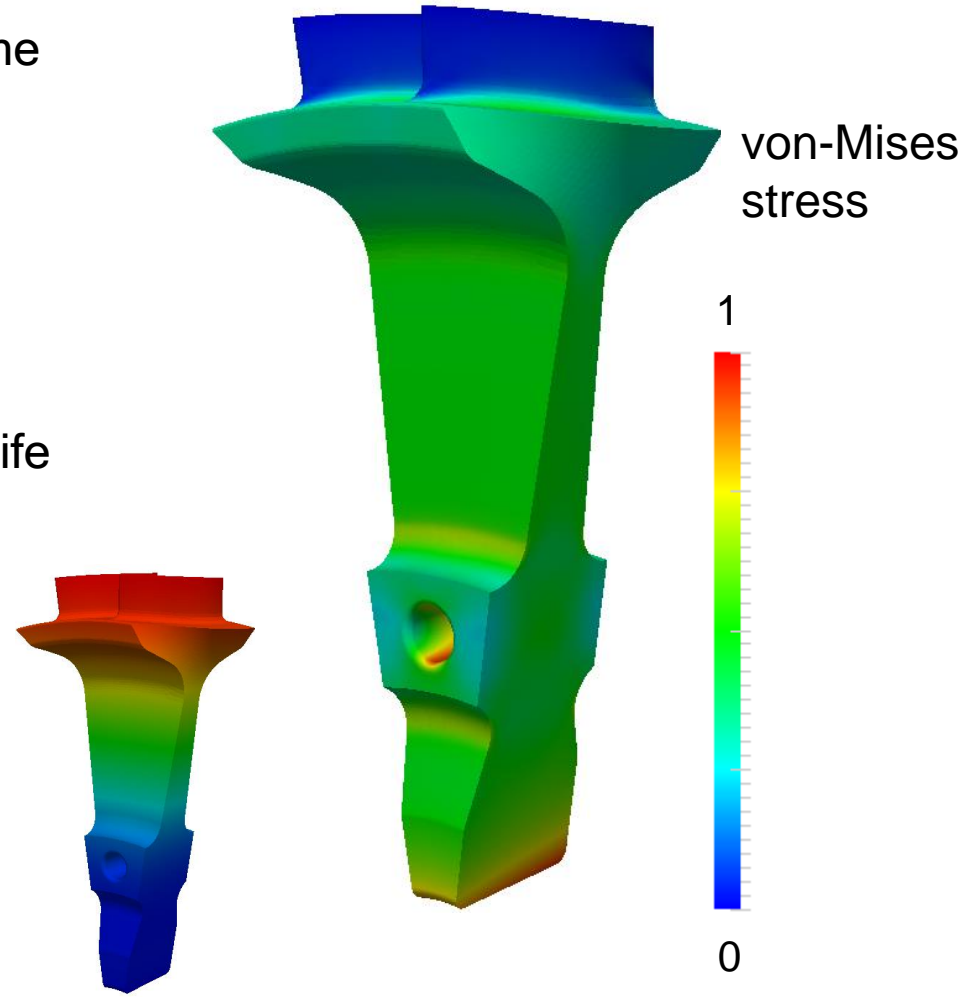


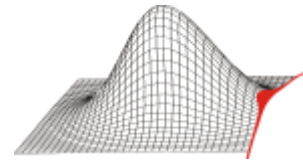


- sensitivity analysis
- system improvement and robustness estimation
- probability of occurrence

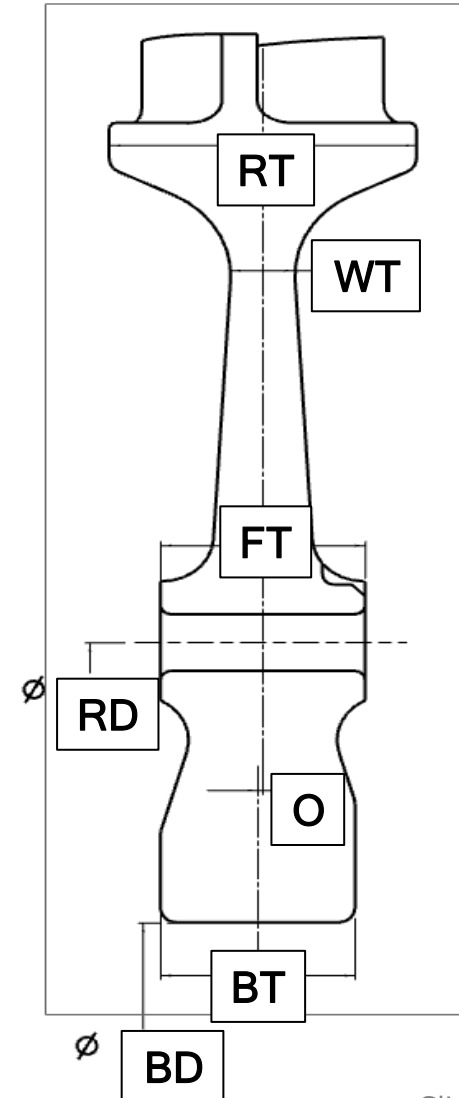


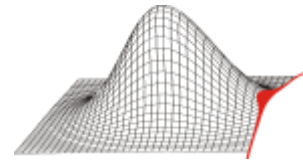
- FE-model provide by MTU Aero Engine
- based on test rig - spin test disc
  - blisk construction
  - material Ti6246
  - integrate dummyblades
  - 39000 rpm
- MTU-internal FE-solver Calculix and life time prediction with MTULife
- elastic analysis, one cycle
- 18° - 3D sector model
- ~ 900 000 nodes
- boundary conditions:
  - axial, tangential fixed
  - loads: rotating speed, radial temperature distribution





- input variables
  - 7 geometrical input parameter
  - uniformly distributed
  - given variation range:
    - manufacturing tolerance
    - range for design improvement
- result parameter
  - von-Mises stress
- Monte Carlo simulation
  - with optimized Latin Hypercube Sampling
  - 60 and 75 realizations
- using the probabilistic tool ProSi





**parametrical  
geometry  
Unigraphics  
NX**

**remeshing**

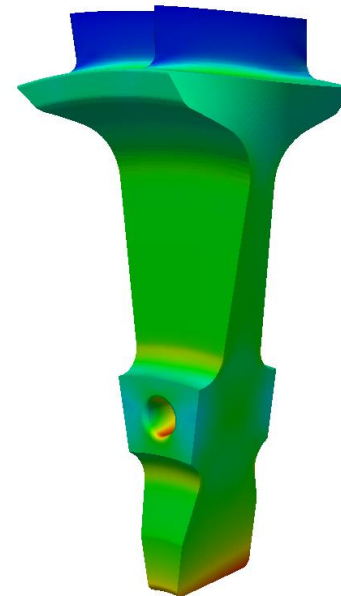
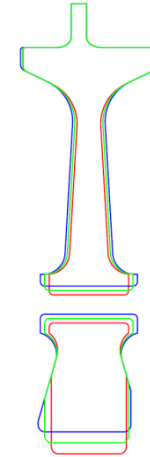
**FE - calculation**

**life time prediction**

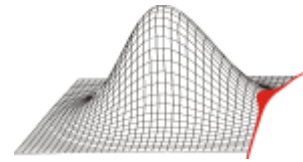
variation file

```
[mm]a1_FT=20  
[mm]a2_BT=19  
[mm]a3_BD=40  
[mm]a4_RT=30  
[mm]a5_TK=103  
[mm]a6_O=0.5  
[mm]a7_WT=6.4
```

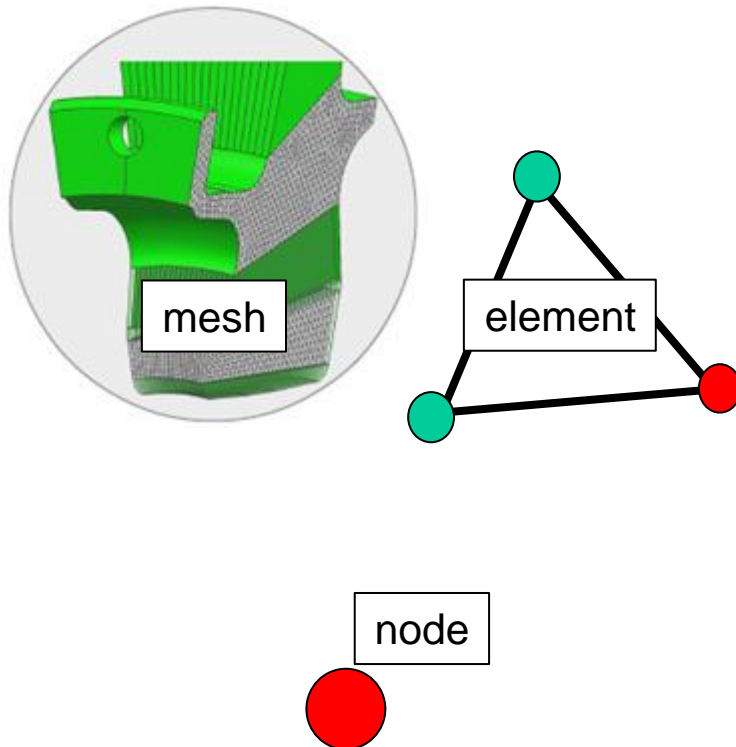
export



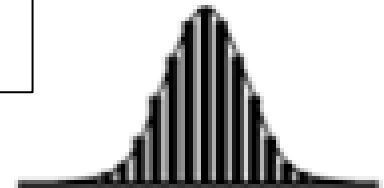




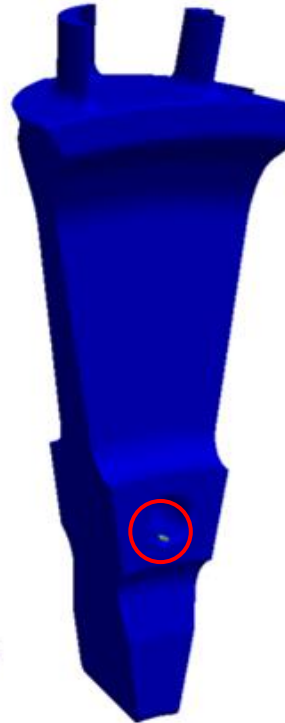
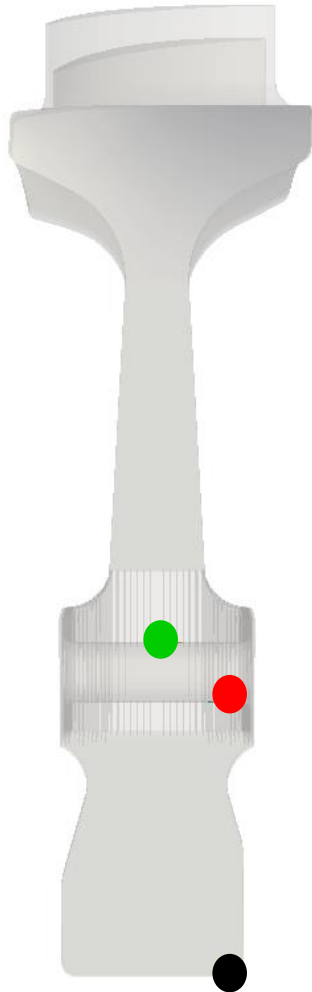
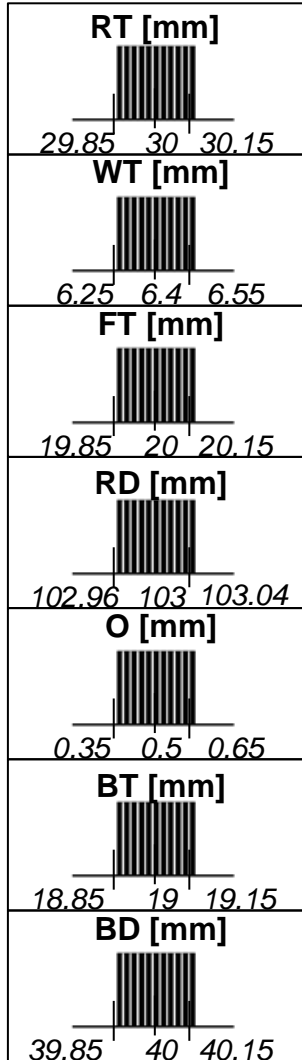
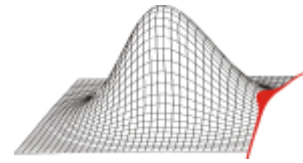
- result transfer of all MCS realizations on the evaluation mesh of a basic geometry



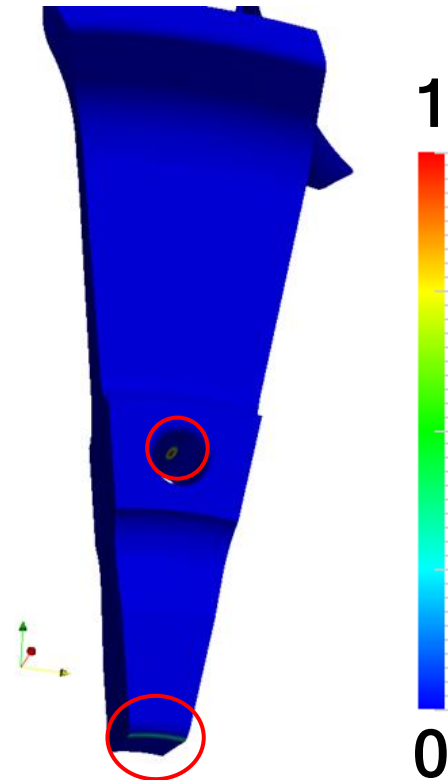
e.g. 50 Mises stress  
values per node



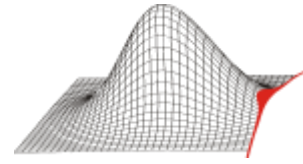
- Calculation of:
  - mean value
  - standard deviation
  - Spearman rank coefficient of correlation
  - relative frequency
  - response surface



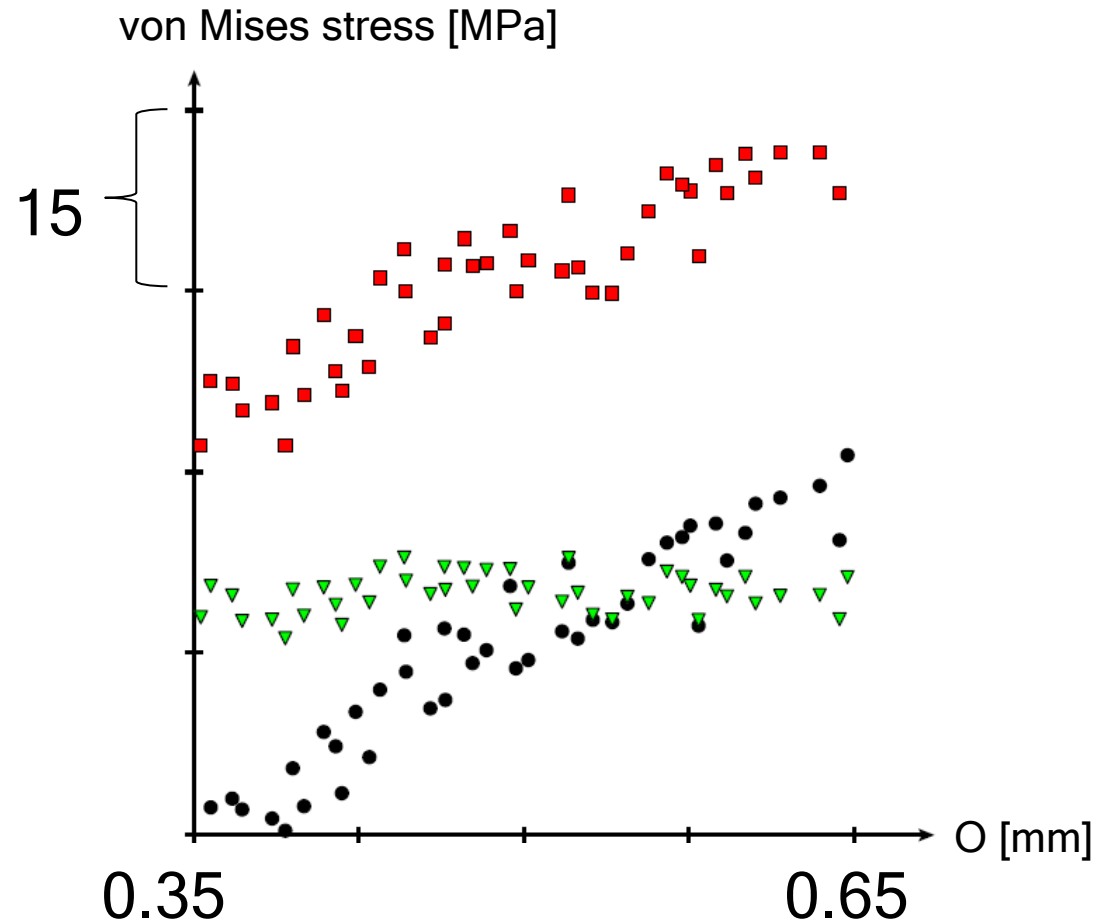
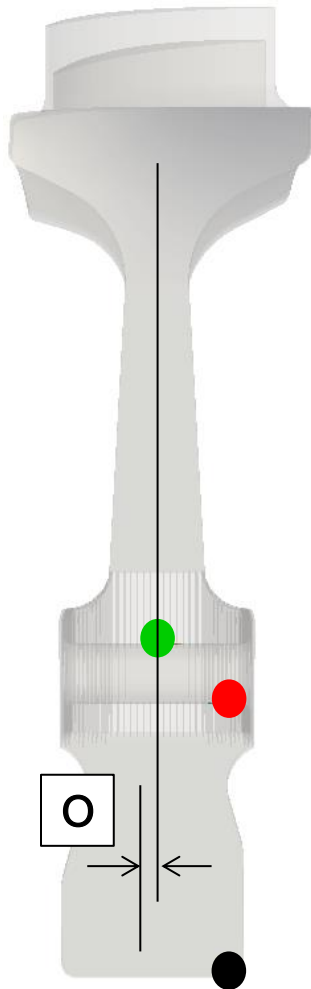
relative frequency:  
von Mises > limit

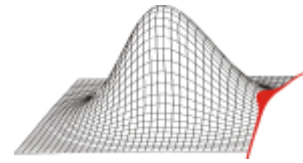






- offset parameter large influence





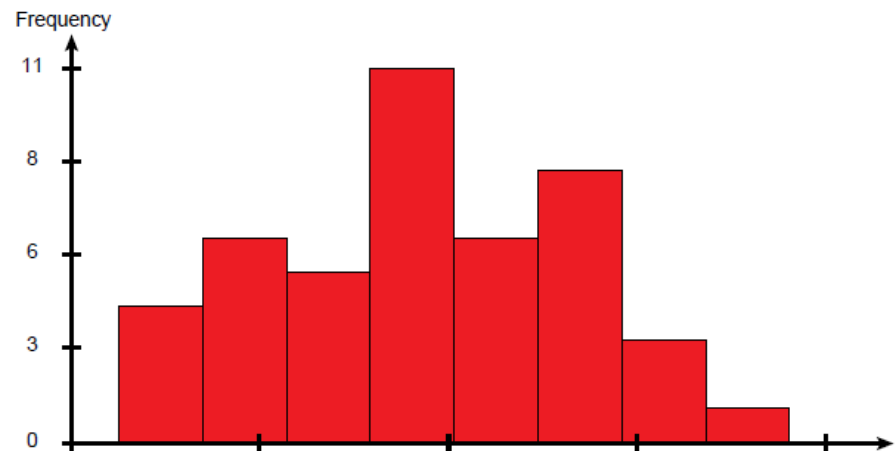
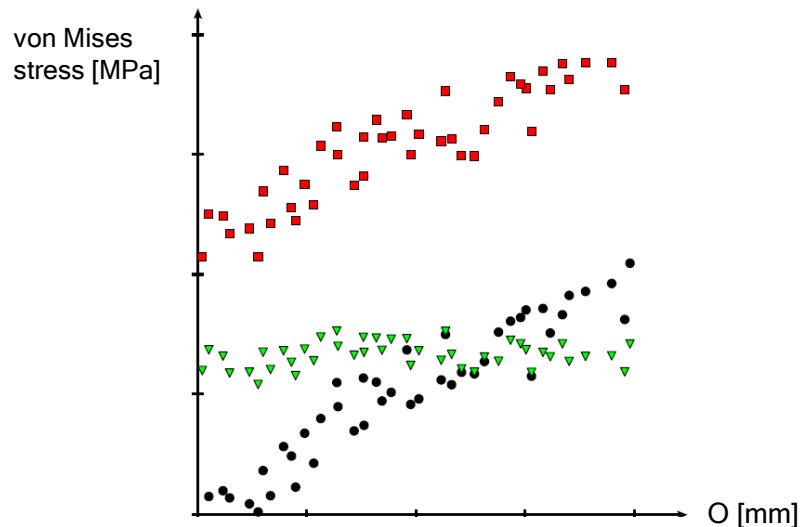
## engineering characteristic

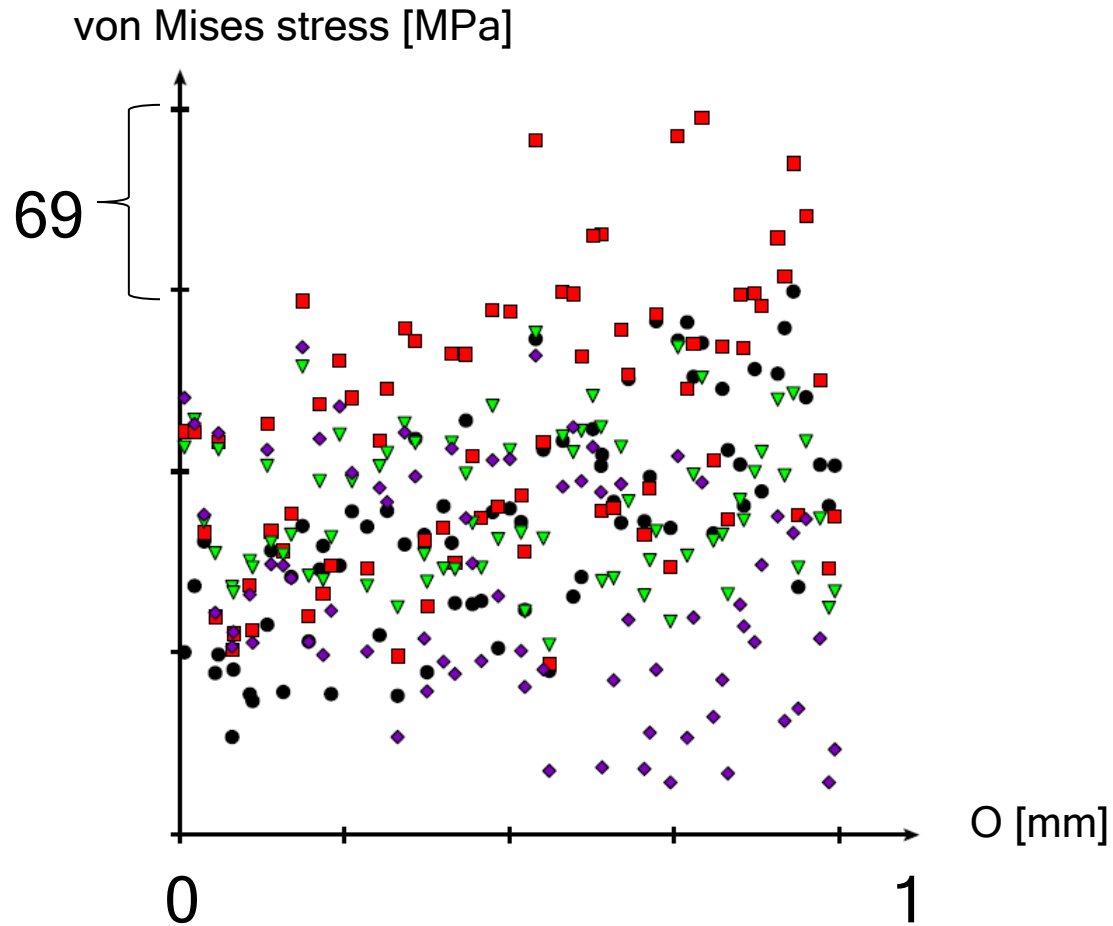
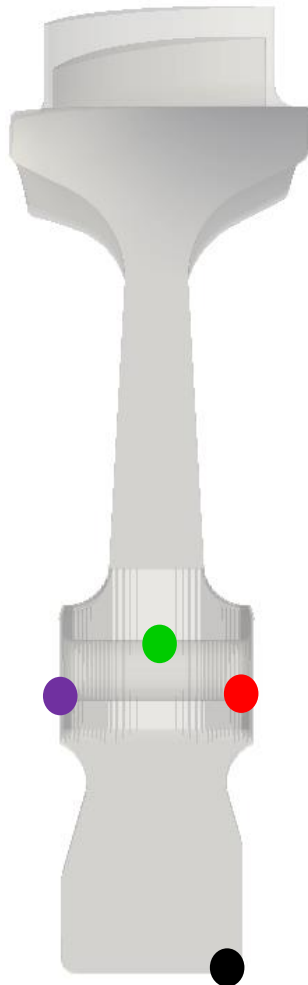
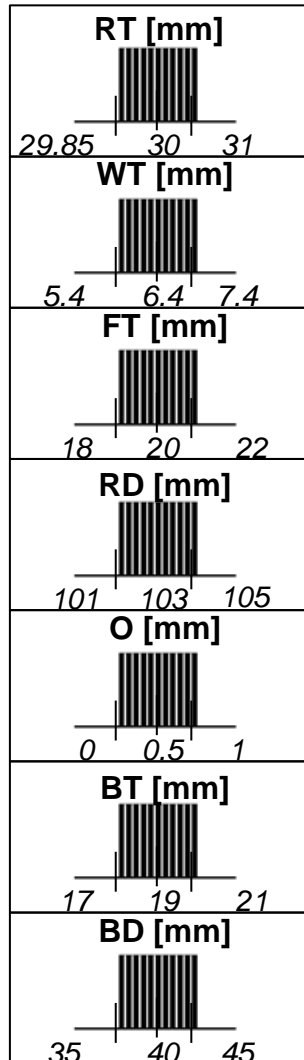
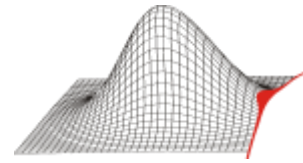
- exceed of limit values
- occurrence of sudden changes in results variables
- occurrence of system instabilities

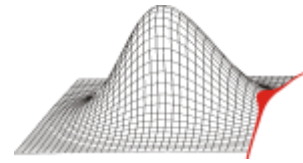
## statistic characteristic

- position of mean value
- amount of the coefficient of variation
  - in results variables

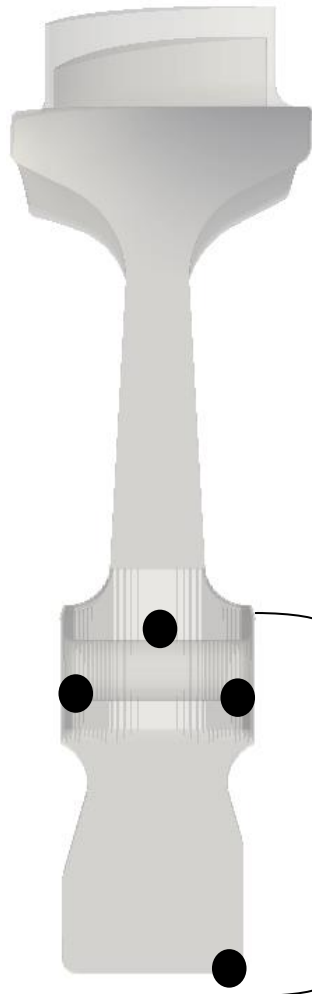
[1]



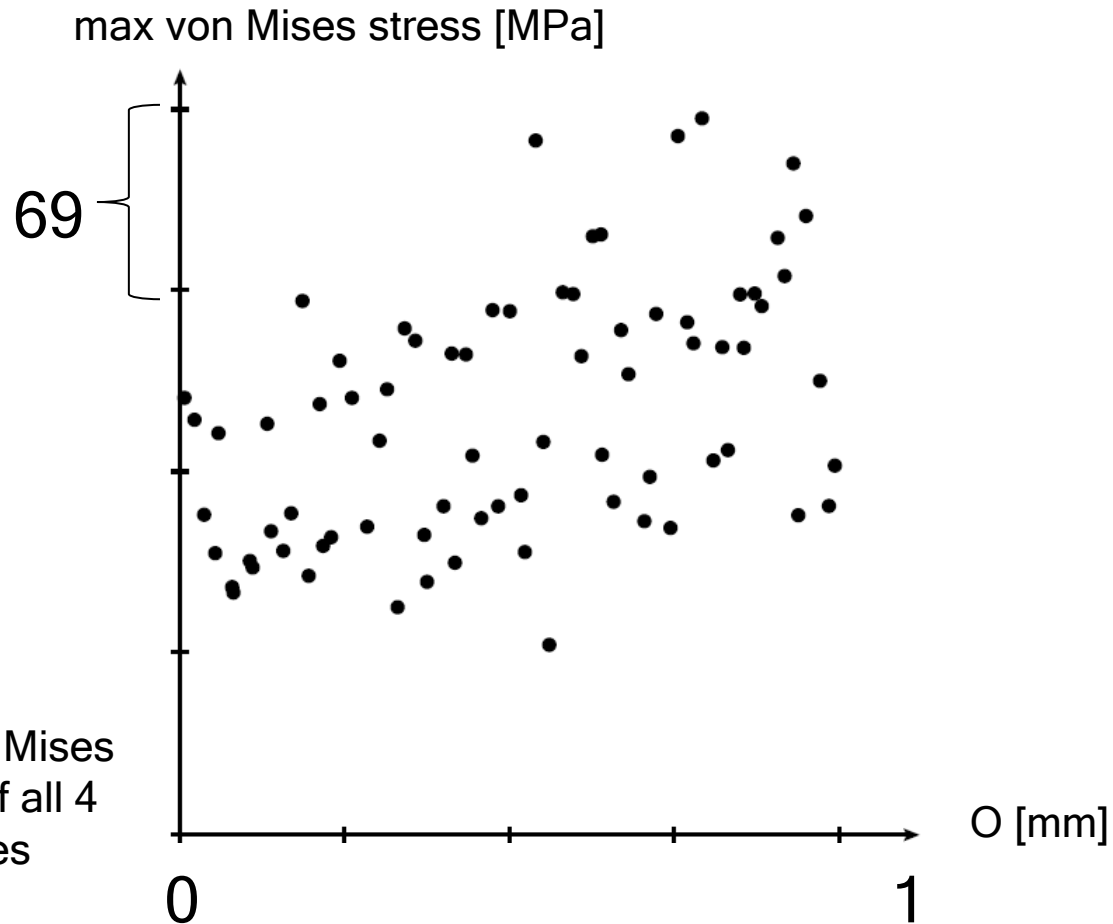


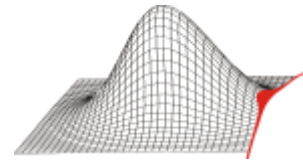


- MCS with variation range for system improvement

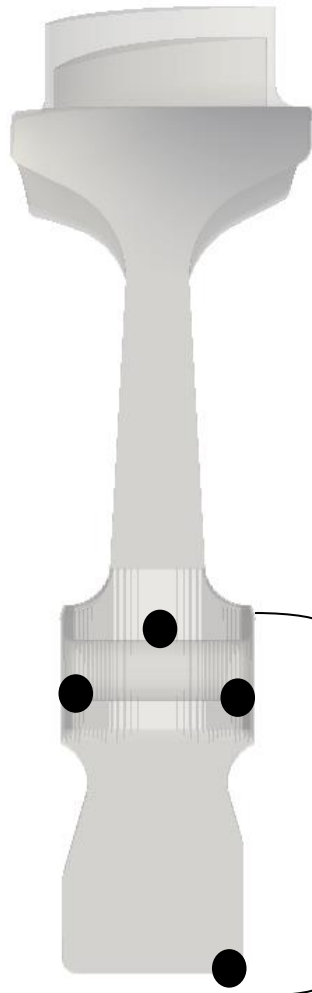


max von Mises  
stress of all 4  
nodes

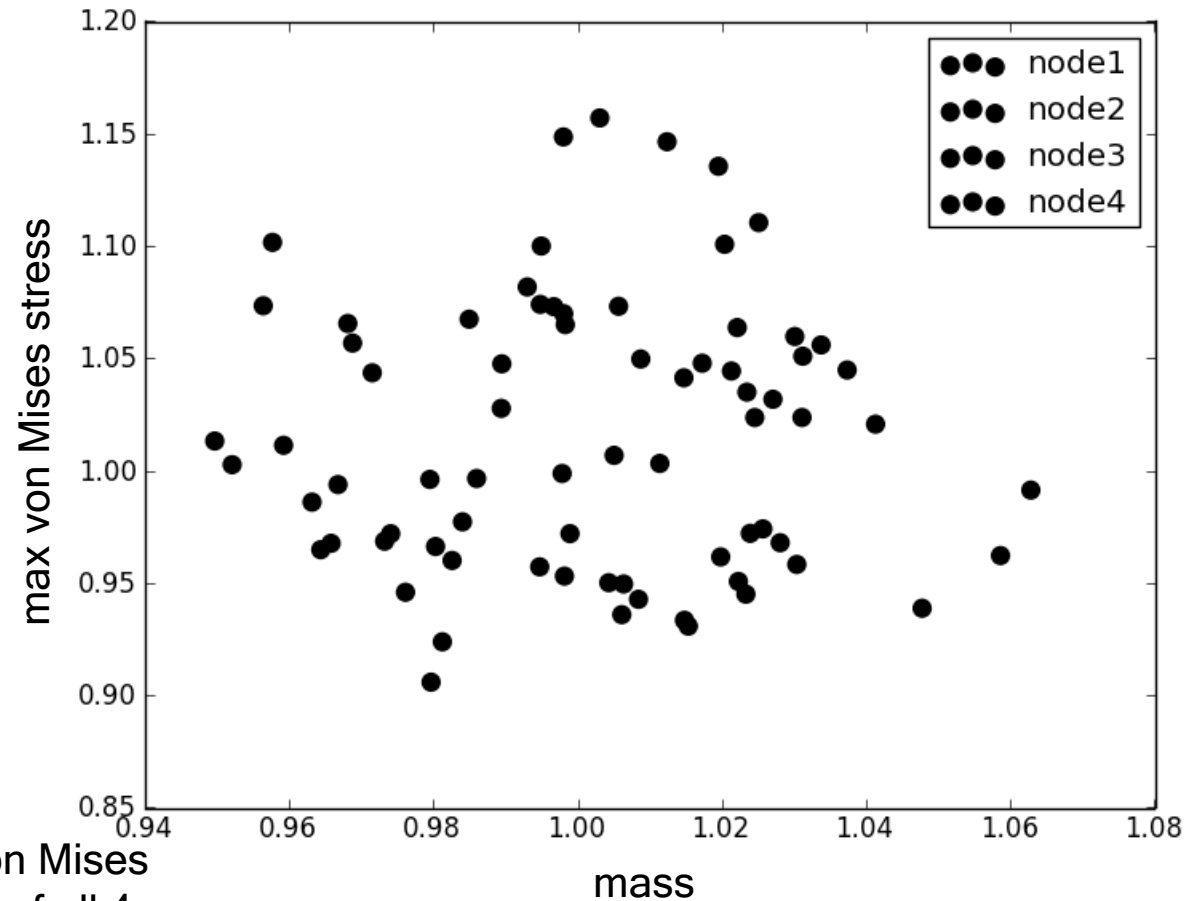


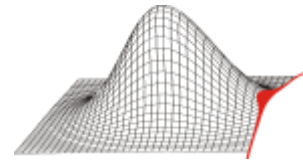


- MCS with variation range for system improvement

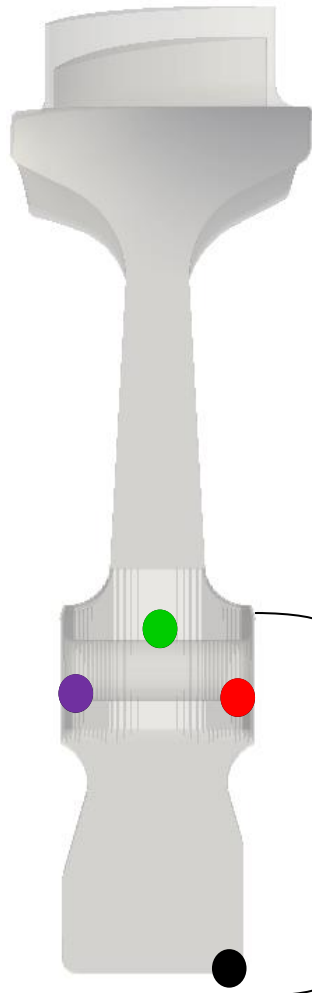


max von Mises  
stress of all 4  
nodes

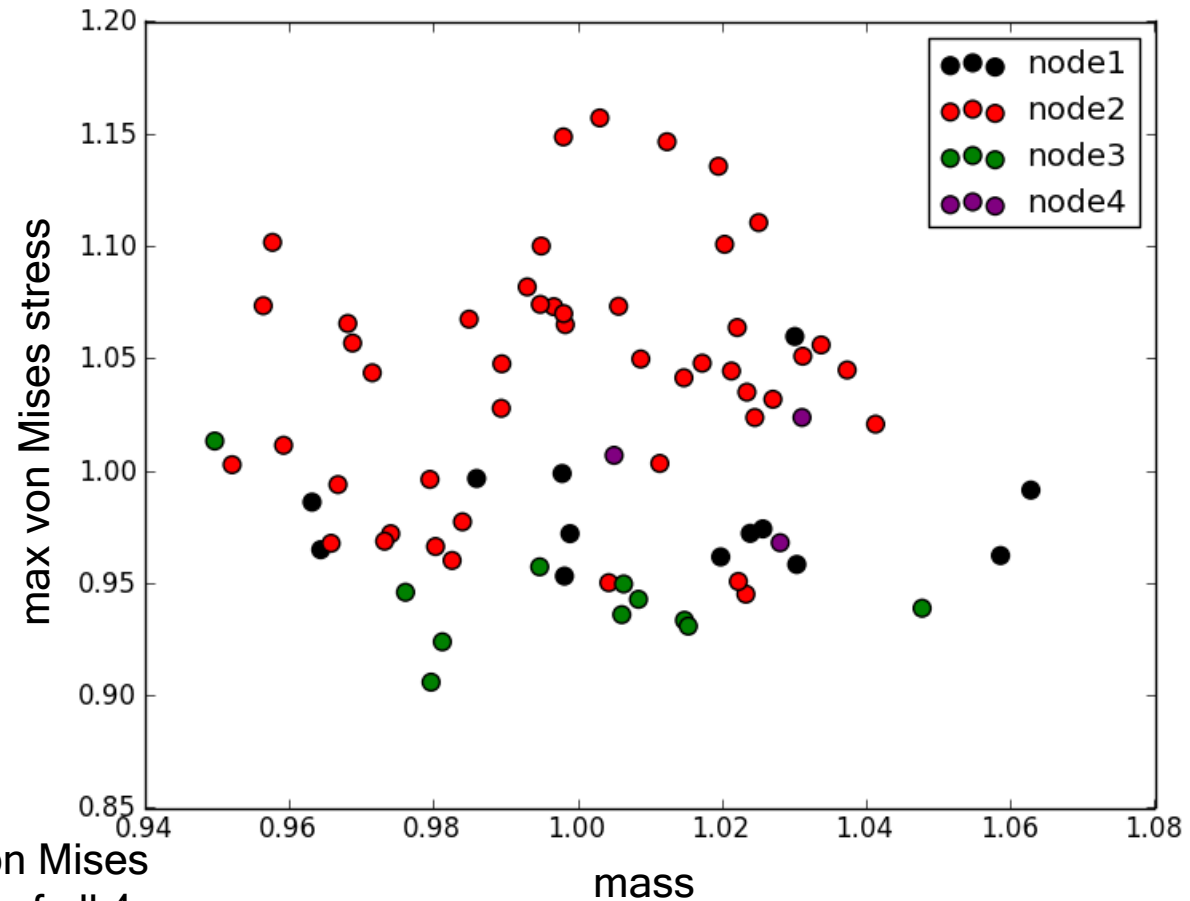


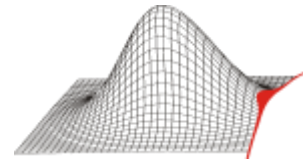


- MCS with variation range for system improvement

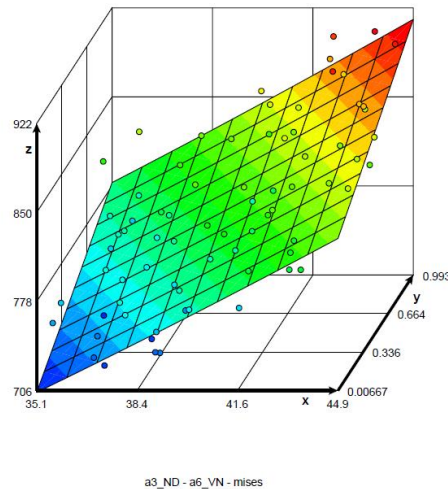
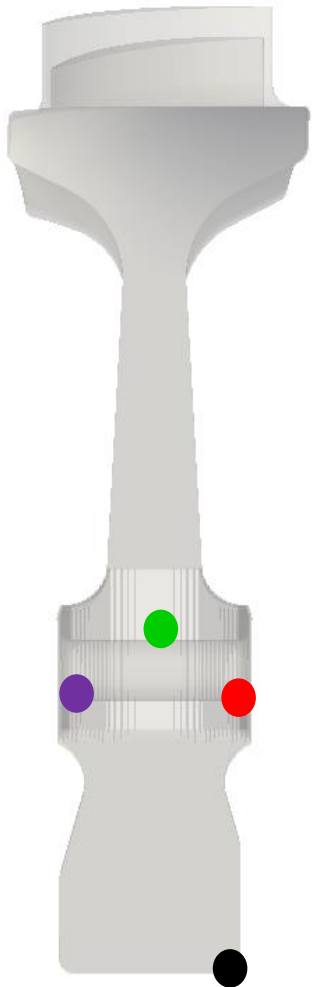


max von Mises  
stress of all 4  
nodes



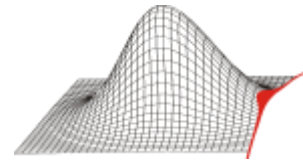


- for each node and rotor disc mass, one metamodel
- first order, linear behaviour

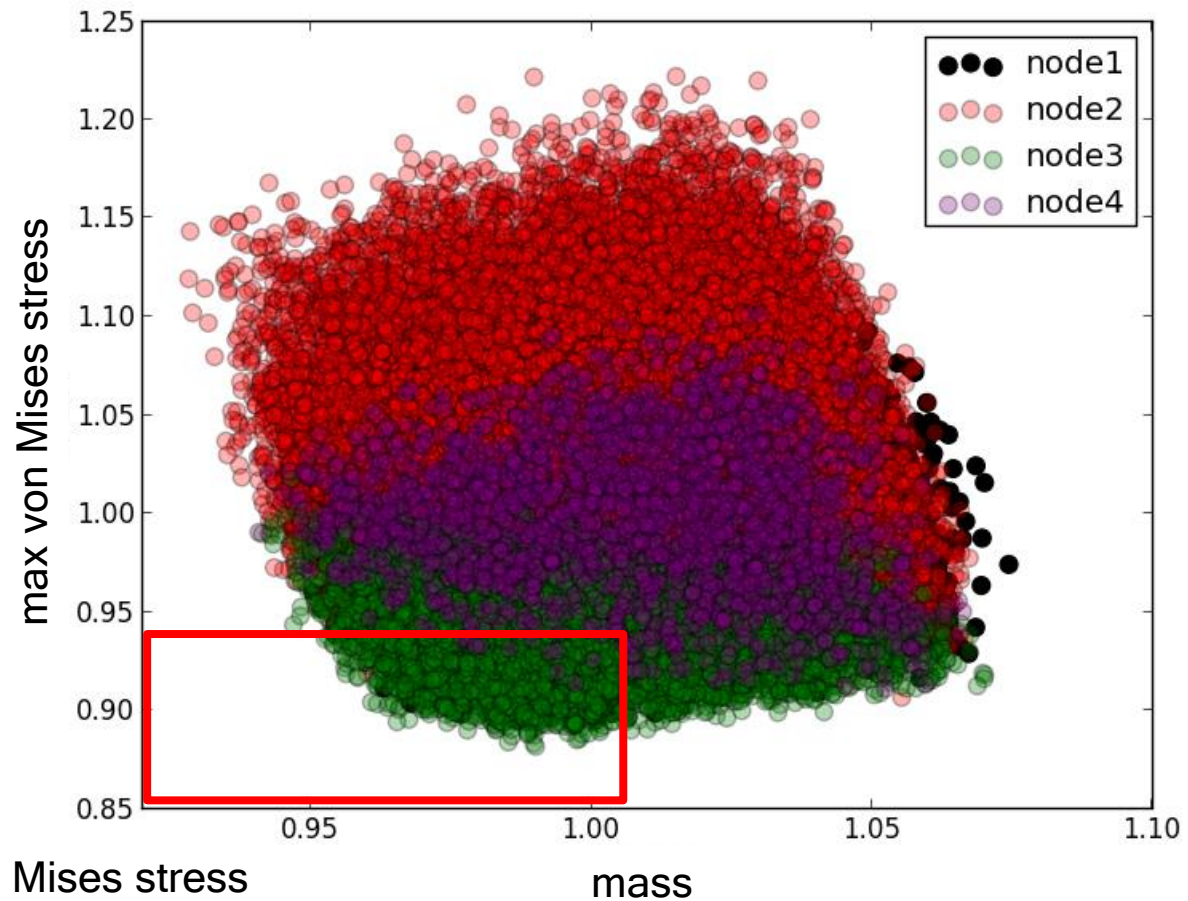
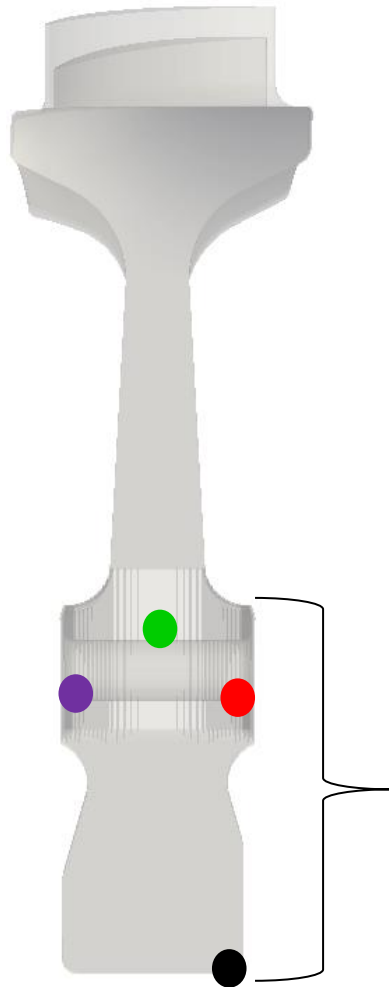


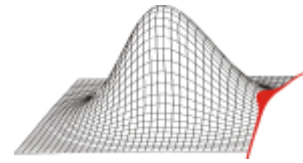
node	delta stress [MPa]	max error [MPa]	R <sup>2</sup>
●	169	10	0.99
●	208	23	0.99
●	118	4	1
●	165	15	0.99
mass	0.0234	2 %	1



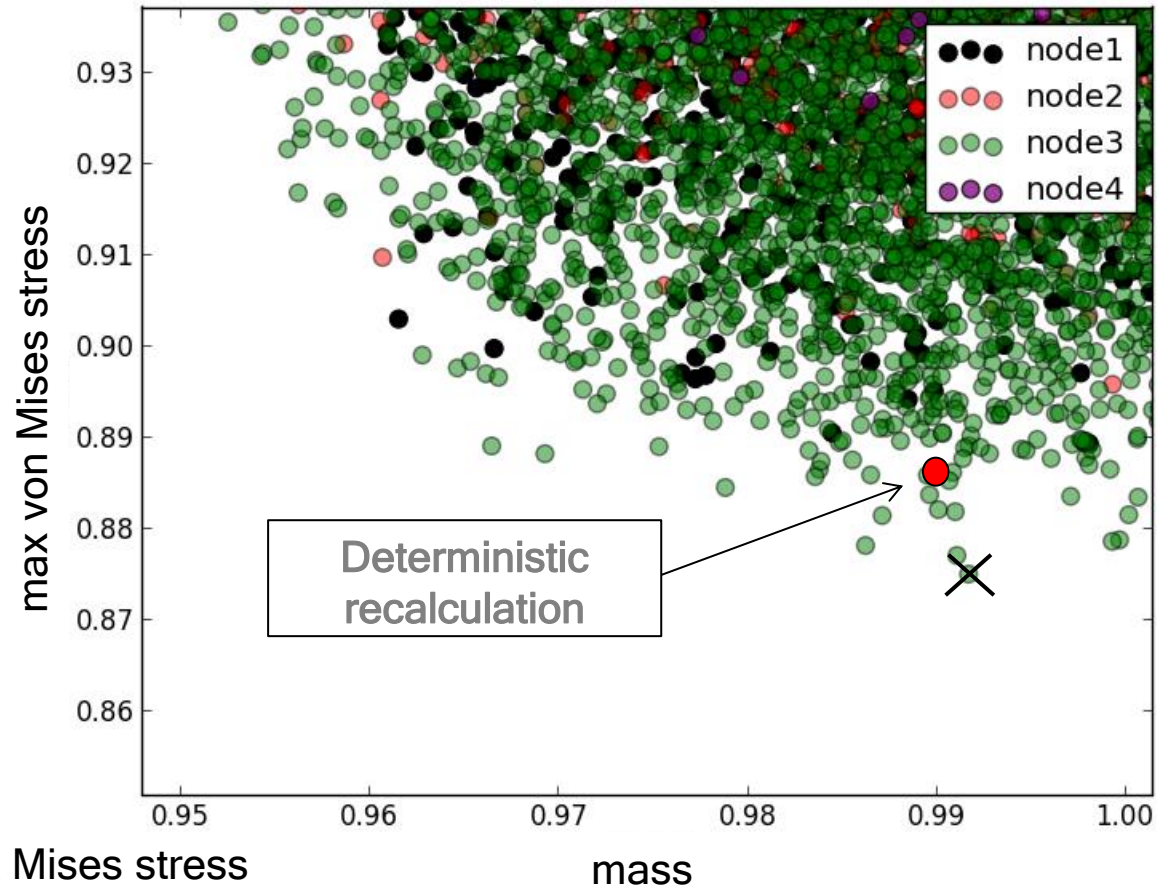
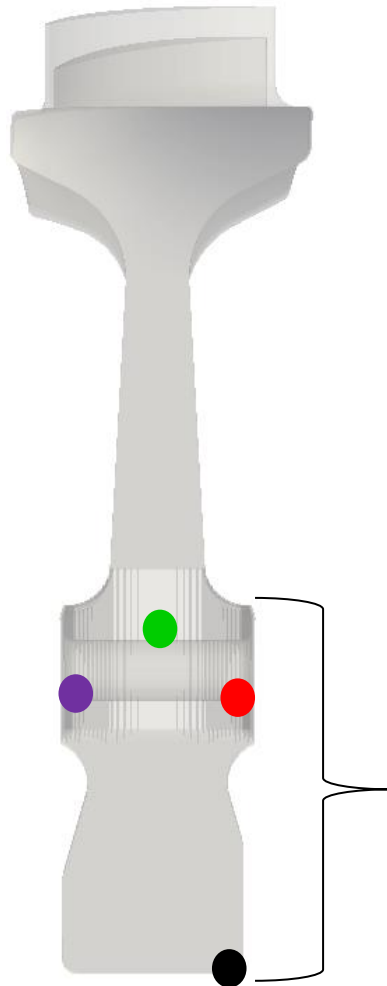


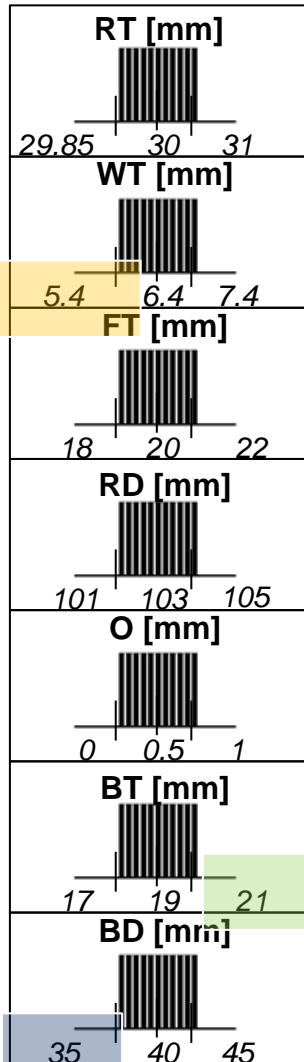
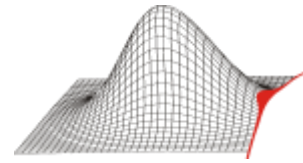
- 50000 shots MCS with variation range for system improvement



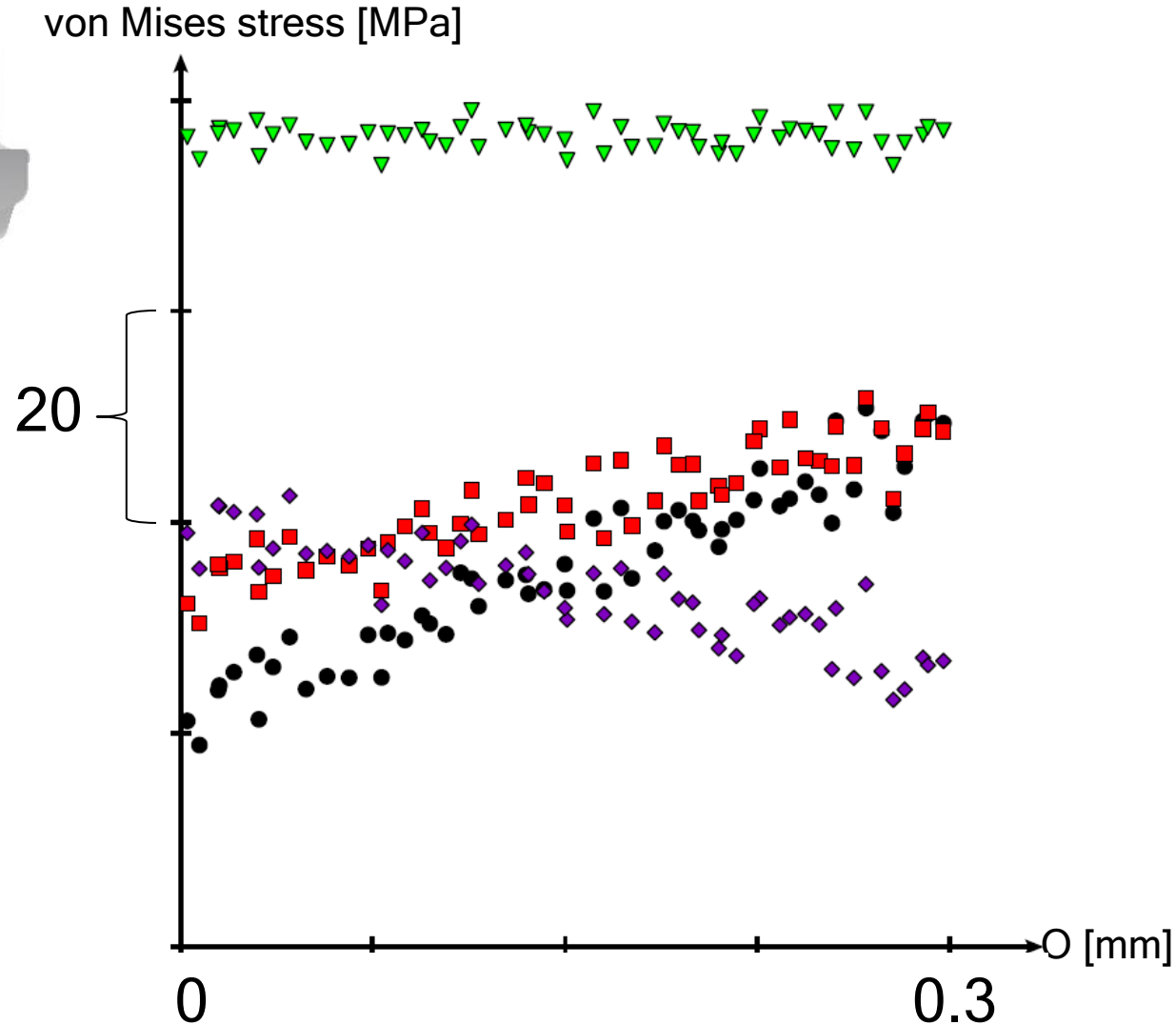
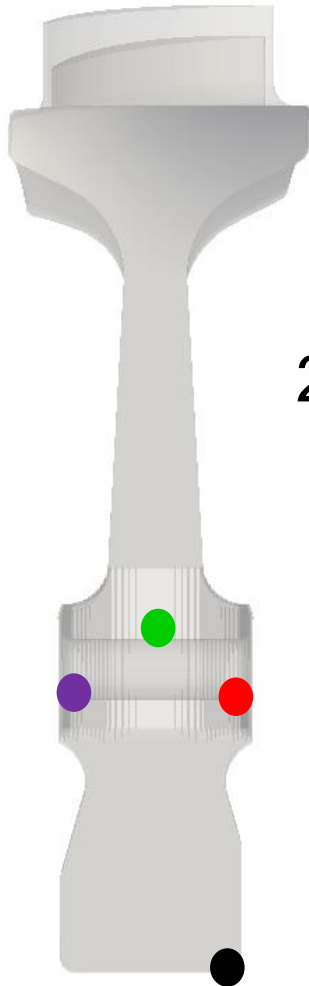
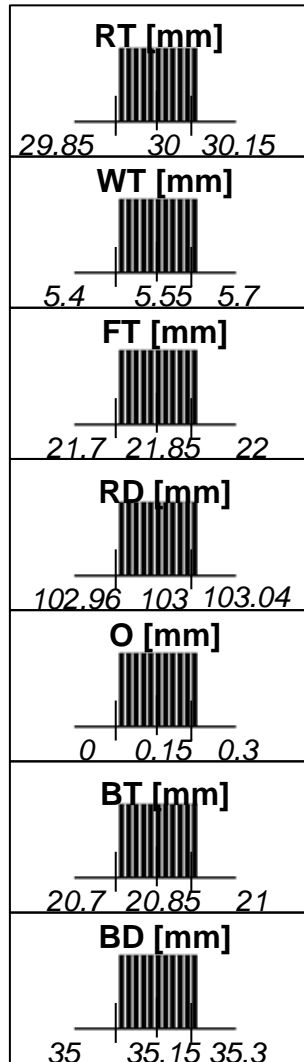
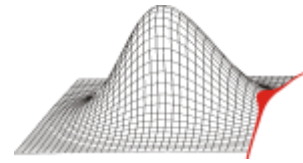


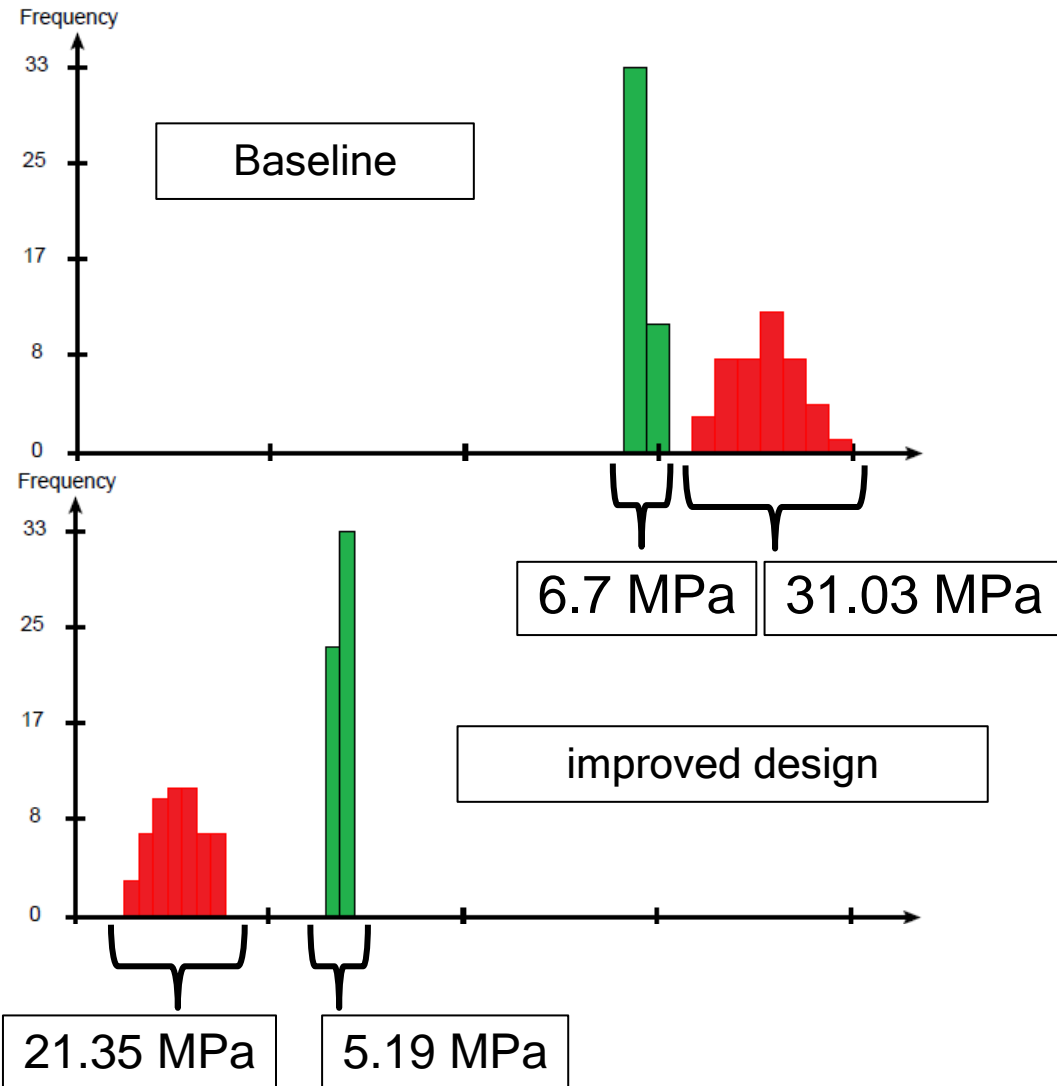
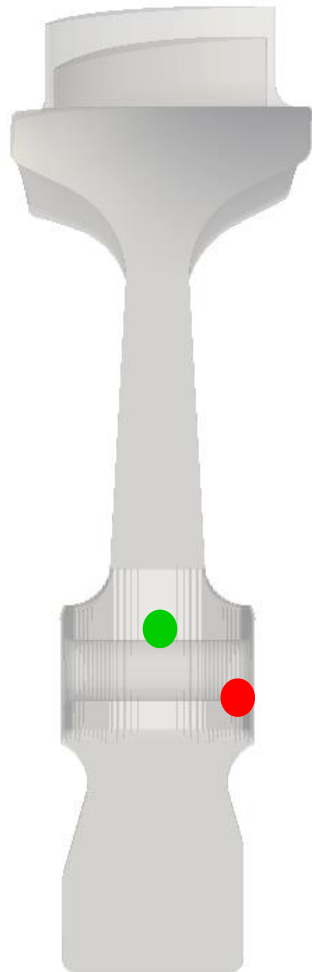
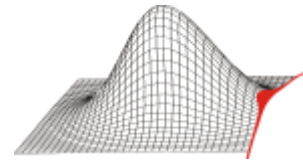
- 50000 shots MCS with variation range for system improvement

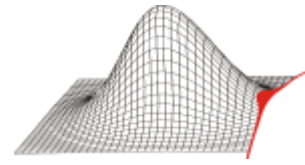




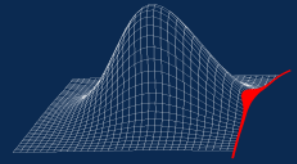
	Baseline	improved design by MCS Metamodell	improved design consider sensitivities
RT	30	30.1044	29.85
WT	6.4	5.42313	5.4
FT	20	21.606	22
RD	103	101.737	103
O	0.5	0.539213	0
BT	19	20.8614	21
BD	40	35.067	35
mass	1	0.9908	0.99167
Mises stress	1	0.8870	0.88468







- implementation of a deterministic automated process chain
- demonstrate a system improvement with all important steps
  - analyse maximum von Mises stress of a base geometry regarding mean value and scatter
  - perform MCS with improvement parameter range
  - improvement of the base geometry with a metamodel
  - Checking the new improved geometry with manufacturing tolerances



# Thank you for your attention!

- [1] WILL, J.; BUCHER, C.: *Statistische Maße für rechnerische Robustheitsbewertungen CAE gestützter Berechnungsmodelle*. Weimarer Optimierungs- und Stochastiktag 3.0, 2006.